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Abstract – Differential Evolution (DE) is a simple, efficient algorithm which has reportedly outperformed many other optimization algorithms in terms of convergence speed and robustness over common benchmark problems and real world applications. However, one is required to set the values of the control parameters of DE for each problem. Such parameter tuning is a time consuming task. The proposed scheme dynamically adapts the mutation step size for better exploration and exploitation of the search space. In this paper we propose SaMSDE algorithm that incorporates exponential distributions to produce mutation steps with varying lengths and suitably adjusts the current step length. To show the performance of our proposed SaMSDE, experiments are carried out on a set of seven well-known benchmark problems. Further the proposed SaMSDE is applied to solve supply chain system. Simulation results show that the proposed algorithm can effectively enhance the searching efficiency and greatly improve the searching quality.

Keywords - Self-Adaptation; Mutation; Differential Evolution; Global Optimization, Supply Chain System

1. Introduction

Global optimization problem is not easy to solve and standard deterministic algorithms tend to stop the search in local minimum nearest to the input starting point. Therefore, heuristic search techniques are widely used by the optimization community when obtaining the global optimum is not only desirable but is also necessary. Such heuristics are often population based search techniques, inspired by some natural process like theory of evolution (Genetic Algorithms, Differential Evolution etc.) or behavior of species (Particle Swarm Optimization, Ant Colony Optimization etc).

Evolutionary algorithms such as Genetic Algorithms (GA) [1] and Differential Evolution (DE) [2][3] are able to find the acceptable solution within a reasonable time limit, but the success of these algorithms depends, to a large extent on the careful tuning of control parameters. In case of DE which is the focus of the present work, the two important parameters are Scaling Factor (F) and Crossover Rate (CR).

Mutation operation plays the most significant role in the performance of a DE algorithm.

Despite having several attractive features, it has been observed that DE sometimes does not perform as per the expectations. Empirical analysis of DE has shown that it may stop proceeding towards a global optimum even though the population has not converged even to a local optimum [5]. The situation when the algorithm does not show any improvement though it accepts new individuals in the population is known as stagnation. Besides this, DE also suffers from the problem of premature convergence. This situation arises when there is a loss of diversity in the population. It generally arises when the objective function is multi objective having several local and global optimums. Like other EA, the performance of DE deteriorates with the increase in dimensionality of the objective function. Several modifications have been made in the structure of DE to improve its performance. One class of modification deals with the development of adaptive control parameters [9] – [15]. Use of self adaptive parameters saves the user from the trouble of fine tuning of parameters,

Many of the developments in DE algorithm design and applications can be found in [15].

In this paper we introduce a new Differential Evolution algorithm SaMSDE, which incorporates exponential distribution to produce mutation steps with varying lengths and suitably adjusts the current step length.

Performance of SaMSDE is analyzed on a set of seven standard unconstrained benchmark functions and a supply chain model.

Optimization of a supply chain model is an integer programming problem or a constrained integer-mixed problem [12]. Several methodologies for optimizing a supply chain have been proposed in the literature so far. Regarding evolutionary algorithms, genetic algorithms are the most popular for supply chain optimization problems [13-18].

The remaining paper is organized as follows: Section II gives a very brief survey of adaptive control parameter

algorithms in DE, an overview of DE is given in the Section III, Motivation for the given work and proposed algorithms are given in sections IV and V respectively. Section VI describes supply chain system in brief. Section VII describes parameter settings, performance metrices and simulation results. Finally the paper concludes with section VIII.

2. Related Work

There are quite different conclusions about the rules for choosing the control parameters of DE. Price and Storn [1] stated that the control parameters of DE are not difficult to choose. On the other hand, Gämperle et al. [6] reported that choosing the proper control parameters for DE is comparatively difficult than expected. Liu and Lampinen [7] reported that effectiveness, efficiency, and robustness of the DE algorithm are sensitive to the settings of the control parameters. The best settings for the control parameters can be different for different functions and the same function with different requirements for consumption time and accuracy. However, there still exists a lack of perfect knowledge on how to find reasonably good values for the control parameters of DE for a given function [8].

Several instances are available in literature for determining the optimal values of these control parameters. But it is observed that mostly the control settings are problem specific and different scholars have different views regarding the optimal values of these parameters [2]-[6]. Researchers therefore laid emphasis on having adaptive/self adaptive control parameters to avoid the careful and time consuming process of fine tuning. Ali and Torn [7] proposed a simple rule for adapting the F scaling factor value during the search process. Quin and Suganthan [9] proposed self-adaptive choice of mutation strategy combined with controlled random adjusting the values of F and CR. Evolutionary self-adaptation of control parameters F and CR suggested by Brest et al. [10][11] have proved good convergence in the applications. Several other modifications have been suggested in the literature [12]-[14].

3. Overview of DE

DE is an Evolutionary Algorithm (EA) proposed by Storn and Price in 1995 [2]. DE starts by randomly

- 1: Generate uniformly distributed random population, G (generation) = 1
- 2: while termination criterion not met do
- 3: for i = 1; $i \le NP$ (Population Size); i = i + 1

Parents Selection

(For Original DE, for each vector x_{i} , select randomly three distinct vectors x_{r1} , x_{r2} and x_{r3} from the current population other than the vector x_i)

4: Randomly select r_1 , r_2 , $r_3 \in \{1, 2, ..., NP\}$, $r_1 \neq r_2 \neq r_3 \neq i$

- 5: for j = 1; $j \le D$ (Dimension); j = j + 1 do
- 6: Randomly select $j_{rand} \in \{1, 2..., D\}$

Binomial Crossover for DE (DE/1/rand/bin)

7: **if** (rand () < CR or $j = j_{rand}$)

8: $u_{ji,G} = x_{r1,G} + F * (x_{r2,G} - x_{r3,G})$

generating an initial population, when no preliminary knowledge about the solution space is available. The uniformly distributed random numbers are evaluated using the fitness function provided. Then the following are executed until maximum number of generation has been reached or an optimum solution is found.

Mutation Operation

For each target vector $x_{i,G}$ at generation G, an associated mutated vector is usually generated as follows: $v_{i,G+1} = x_{r1,G} + F(x_{r2,G} - x_{r3,G})$ (1) where r_1 , r_2 , $r_3 \in (1,2...,NP)$ are randomly chosen integers, different from each other and also different from the running

different from each other and also different from the running index i. F is a real and constant factor having value between [0, 2] and controls the amplification of differential variation $(x_{r2, G} - x_{r3, G})$.

Crossover Operation

After the mutation phase, the "binominal" crossover operation is introduced in order to increase the diversity of the perturbed parameter vectors. The parent vector is mixed with the mutated vector to produce a trial vector $u_{ji,G+1}$,

$$\cdot u_{ji,G+1} = \begin{cases} v_{ji,G+1} & \text{if } rand_j(0,1) \le Cr \forall j = k \\ x_{ji,G} & \text{otherwise} \end{cases}$$
(2)

where j, k = {1, 2,..., D (dimension)}; k is the random parameter index, chosen once for each i, $rand_j \in [0, 1]$ and Cr is a user-specified crossover constant in the range [0, 1].

Selection Operation

Finally selection takes place where a tournament is held between the target vector and trial vector and the one with better fitness function is allowed to enter the next generation. In this way individuals in a new generation are as good as or better than the individuals in the previous generation. DE contains 4 parents, in which one is target vector; x_i and three are random vectors x_{rl} , x_{r2} and x_{r3} . The detailed pseudocode is given in Figure 1 and process is shown in Figure 2. 9: else 10: $u_{ji,G} = x_{ji,G}$ 11: end if 12: end for 13: end for 14: **for** i = 1; $i \le NP$; i = i + 1 *do* ***** Selection $\mathbf{if}\,f(u_{ji,G})\leq f(x_{i,G})$ 15: 16: $x_{i,G+1} = u_{ji,,G}$ 17: else 18: $x_{i,G+1} = x_{i,G}$ 19: end if ***** 20: end for 21: G = G + 1

22:end while



Pseudocode of basic DE



Figure 2. Process of DE

4. Motivation

The basic motivation behind the proposed algorithm SaMSDE is to balance the exploration and exploitation in basic DE. So, the proposed algorithm incorporates exponential distributions to produce mutation steps with varying lengths and suitably adjusts the current step length. Mutation with large step size is likely to produce large variations which would facilitate better exploration of the undiscovered regions of the search space while small step size usually produces small variations that are better for exploitation of the already found solutions. The appropriateness of small or large steps changes dynamically depending on the current stage and maturity of the ongoing search process as well as the properties of the search space. So, dynamic adaptation of mutation step size is quite promising and efficient to solve continuous optimization problems.

5. Self Adaptive Mutation Step size

The only structural difference between the proposed SaMSDE algorithm and the basic DE is during mutation. The scaling factor (F) in eq. (1) is replaced by $MS_{ij} * r_{ij}$.

$$v_{i,G+1} = x_{r1,G} + MS_{ij} * r_{ij} (x_{r2,G} - x_{r3,G})$$
(3)

 MS_{ij} is the scaling factor that keeps the knowledge of separately for every dimension, j of every individual x_i , r_{ij} randomly range in [0, 1].

 MS_{ij} is initialized to 1 during the beginning of the search process. As the search progresses across several local

minima and plateaus or flat regions, the MS_{ii} values are automatically adjusted by the adaptation scheme in order to take care of the current situation. Large values for MS_{ij} would expand the product $MS_{ii} * r_{ii}$ in order to promote large mutation steps for better exploration of the search space and quickly get rid of local minima. On the contrary, small values (less than unity) for MS_{ii} would shrink the product $MS_{ij} * r_{ij}$ (in (3)) and thus facilitate small mutation steps ensuring exploitation in the vicinity of current search points. Whether exploitation or exploration would be better at current search stage might not be apparent or could not be predicted beforehand. So SaMSDE employs two different exponential distributions in order to produce different range of scaling factor (i.e. MS_{ij}) values for explorations and exploitations. The adjusted scaling factors (i.e., MS_{ii} values) are the weighted average of the current scaling factor values and the random values generated anew from the two exponential distributions. The procedure is further explained in the following pseudocode (Figure.4) along with the two distributions used for explorations and exploitations. To adapt the MS_{ij} values, SaMSDE generates two gaussian random values, r[1] and r[2] from the ranges (0, -10] and (0, 10]. Now, for every individual solution two different offspring solutions are generated by (3): by using $MS_{ij, 1} = 2^{r[1]}$ and $MS_{ij, 2} = 2^{r[2]}$. Since r[1] < 0 and r[2] > 0, the scaling factor $MS_{ij,1} = 2^{r[1]}$ would generate small steps for better exploitation, while $MS_{ii,2}$ = $2^{r[2]}$ would produce large steps for more search space exploration. SaMSDE evaluates the fitness of each offspring and accepts the better one. Also, it moves MS_{ii} from its current value to the new scaling factor (MS_{ij,1} or MS_{ij, 2}) based on which one produces better offspring using the formula:

 $SF_{ij} = r_1 * MS_{ij} + (1 - r_1) * MS_{ij, K}$ (4) where r1, r2 \in rand[-0.5, 0.5]. These two distributions produce the scaling factor values for exploration and exploitation respectively. Exponential distributions provide wide range of values as scaling factors

facilitating very small to very large jumps ensuring from

little to large explorations and exploitations. 1. Follow Steps 1 to 4 from Figure 1. 2. for each $i \in NP$ 3. for j = 1 to D { 4. for k = 1 to 2 { 5. $r[k] = rand[0, \tau_k]$ 6. $MS_{ij,k} = 2^{r[k]}$ 7. $v_{ij,k} = v_{ij}$ computed from (3) by using $MS_{ij} = MS_{ij,k}$ 8. $temp_v_i = v_i$, but v_{ij} replaced by $v_{ij,k}$ 9. $f[k] = f(temp_v_i)$ 10. find k such that f[k] is the minimum over $f[temp_v_i]$ 11. Calculate MS_{ij} using eq. (4) } 12. Follow steps 5 to 22, but replace step 8 by eq. (3) Figure 3. Pseudocode for the adaptation of

6. Self Adaptive Mutation Step size

mutation step size in DE

Experimental Setting

In this section, the proposed SaMSDE algorithm is validated on a set of seven benchmarks taken from [17]. In order to investigate the performance of the proposed SaMSDE we compared it with the DE algorithm and PSO. DE, proposed SaMSDE are implemented in Dev-C++ and the experiments are conducted on a computer with 2.00 GHz Intel (R) core (TM) 2 duo CPU and 2- GB of RAM. In order to make a fair comparison of DE and the proposed algorithm, we fixed the same seed for random number generation so that the initial population is same for both the algorithms. For each problem, the SaMSDE is independently run 30 times. The parameter setting is taken as follows:

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Mutation strategy	DE/rand/1/bin
Population size NP	50
Scaling factor (F)	0.5
Crossover probability	0.9
Iterations	5000
Value to Reach (VTR)	10-06
Maximum NFE	300000

Performance Criteria

Four performance criteria are selected to evaluate the performance of the algorithms. These criteria are described as follows:

Mean Fitness and Standard Deviation

The average of function fitness value that an algorithm can find, using predefined maximum NFEs, is recorded in each run and then average of the function fitness values are calculated. Also the average and standard deviation of the fitness values are calculated.

NFEs [18]

The number of fitness function evaluations (NFEs) is recorded when the VTR is reached before to reach maximum NFE. i.e we set the termination criteria as $\left|f_{optimal} - f_{global}\right| \leq VTR$ and record average NFE of successful run over 30 runs.

Convergence Graphs [18]

The convergence graphs show the mean fitness performance of the total runs, in the respective experiments.

Acceleration rate (AR) in % [19]

This criterion is used to compare the convergence speeds between SaMSDE and DE. It is defined as follows:

$$AR = \frac{NFE_{one\ a\ lg\ orithm} - NFE_{other\ a\ lg\ orithm}}{NFE_{one\ a\ lg\ orithm}} \%$$
(5)

Simulated Results

The simulated results based on the above experimental setting are given in Table-1, Table-2 and Table-3. In Table-1 we have taken the results on the basis of average error. In this case NFEs are fixed at 105 to estimate the average of minimum fitness function value in 30 runs. From the Table-1 it can be clearly observed that for all benchmark functions SaMSDE gives better results than PSO and DE. A two tail sample t-test [20]-[21] is also applied to analyze the statistical significance of the proposed algorithm. We have checked the significant difference of SaMSDE with respect to DE at 5% level of significance. For statistical analysis, we consider the null hypothesis and alternative hypothesis as:

 H_0 : There is no significant difference between the mean fitness value of SaMSDE and others algorithms.

 H_1 : Mean fitness value of SaMSDE is better than others algorithms.

The calculated t-value of all function is greater than t-table value that shows the significant better performance in the comparison of DE.

In the Table-2, we fixed VTR as given in experimental setting and then calculated the average NFE of 30 runs. From Table-2 we can see that the proposed SaMSDE gives the better results for every function in the comparison to the other algorithms. From the Table-2 it is clear that the proposed SaMSDE is faster than PSO & DE by 39.96% & 29.33% respectively. Best and worst function values in 30 runs are shown in Table-3.

Figure 4(a)-(b) shows the convergence graph of SaMSDE with the comparisons of DE and PSO. NFEs taken to estimate the average of minimum fitness function value in 30 runs are also presented graphically in Figure 5.

Table 1. Comparison of SaMSDE with PSO, DE algorithm in terms of NFEs and AR(%), Here 3/1 implies SaMSDE vs PSO, and 3/2 implies SaMSDE vs DE

PSO, and 3/2 implies SaMSDE vs DE								
PS()	DE	SaMSDE	AR	(3/1)	AR (3/	'2)	
436	00	26380	16360	62.477064		37.983321		
976	97630 74370		62890	15.097818		15.436332		
468	200	330840	160600	65.698419		51.456898		
618	80	76680	54362.5	12.148513		29.104721		
291	10	19500	17880	38.577808		8.3076923		
532	20	52590	37190	30.1	120256	29.283134		
500	40	33540	22220	55.5	595524	33.750745		
erage	AR((%)		39.9	96	29.33		
Tab	le 2.]	Best and (V	Worst) Funct	tion v	alues in	30 runs		
F		PSO	DE		SaM	SDE		
Б	6.04453e-005 0.000100962		8.69549e-	8.69549e-005		8.33852e-005		
1.1			0.000100901		0.00010096			
F.	5.56861e-006		6.06769e-005		4.78849e-006			
1.5	9.98	8884e-006	9.44291e-	005	9.9399	5e-006		
F.	0.00993023		0.000685359		0.086481			
13	0.0100924		0.00099867		0.0987919			
F.	7.86592e-005		4.68213e-	e-006 5.57		4e-006		
14	9.89	9971e-005	9.74202e-	006	7.7909	9e-006		
F.	0		0		0			
15	0		0		0			
E.	8.73	398e-005	8.79372e-	005	8.8052	6e-005		
10	0.00	00100506	9.95211e-	005	0.0001	00549		
F ₇	9.19	9165e-005	9.12616e-	006	2.3705	9e-005		
• /	0.00	0100997	0.0001000)94	9.8977	2e-005		
	$\begin{array}{c} \textbf{PSC} \\ 436 \\ 976 \\ 468 \\ 618 \\ 291 \\ 532 \\ 500 \\ \textbf{F} \\ \textbf{F} \\ \textbf{F}_1 \\ \textbf{F}_2 \\ \textbf{F}_3 \\ \textbf{F}_4 \\ \textbf{F}_5 \\ \textbf{F}_6 \\ \textbf{F}_7 \end{array}$	$\begin{array}{c c} PSO \\ \hline PSO \\ \hline 43600 \\ 97630 \\ \hline 43600 \\ 97630 \\ \hline 0040 \\ \hline 0040 \\ \hline 0040 \\ \hline 0070 \\ \hline $	$\begin{array}{c c c c c c c c c c c c c c c c c c c $	PSO, and 3/2 implies Sa PSO DE SaMSDE 43600 26380 16360 97630 74370 62890 468200 330840 160600 61880 76680 54362.5 29110 19500 17880 53220 52590 37190 50040 33540 2220 erage AR(%) Table 2. Best and (Worst) Funct F PSO DE F1 6.04453e-005 8.69549e- 0.000100962 0.0001009 F2 5.56861e-006 6.06769e- 9.98884e-006 9.44291e- F3 0.00993023 0.0006853 0.0100924 0.0009986 F4 7.86592e-005 4.68213e- 9.89971e-005 9.74202e- F5 0 0 F6 0.000100506 9.95211e- F7 9.19165e-005 9.12616e- F7 9.19165e-005 9.12616e-	PSO, and 3/2 implies SaWSD PSO DE SaMSDE AR 43600 26380 16360 62.4 97630 74370 62890 15.0 468200 330840 160600 65.0 61880 76680 54362.5 12.1 29110 19500 17880 38.5 53220 52590 37190 30.1 50040 33540 22200 55.5 erage AR(%) 39.9 Table 2. Best and (Worst) Function with the set and (Wor	PSO, and 3/2 implies SalvisDE vs DE PSO DE SaMSDE AR (3/1) 43600 26380 16360 62.477064 97630 74370 62890 15.097818 468200 330840 160600 65.698419 61880 76680 54362.5 12.148513 29110 19500 17880 38.57808 53220 52590 37190 30.120256 50040 33540 2220 55.59524 Pron 39.6 Table 2. Best and (Worst) Functor values in F 9.9 6.0 0.0 F_1 $6.04453e-005$ $8.69549e-005$ 8.3385 0.000100962 0.000100901 0.0001 0.0001 F_2 $5.56861e-006$ $6.06769e-005$ 4.7884 F_3 0.00093023 0.000685359 0.0864 0.0100924 0.00099867 0.0987 F_4 $7.86592e-005$ $4.68213e-006$ 5.5705 <td>PSO, and 3/2 implies SaWSDE vs DE PSO DE SaMSDE AR (3/1) AR (3/2) 43600 26380 16360 62.477064 37.983 97630 74370 62890 15.097818 15.436 468200 330840 160600 65.698419 51.456 61880 76680 54362.5 12.148513 29.104 29110 19500 17880 38.577808 8.3076 53220 52590 37190 30.120256 29.283 50040 33540 22200 55.59524 33.750 PSO DE 29.33 Table 2. Best and (Worst) Functor values in 30 runs F PSO DE SaMSDE F_1 6.04453e-005 8.69549e-005 8.33852e-005 0.000100901 0.00010096 F_2 5.56861e-006 6.06769e-005 4.78849e-006 9.93975e-006 F_3 0.00093023 0.00085359 0.086481 0.00993023 0.00089867</td>	PSO, and 3/2 implies SaWSDE vs DE PSO DE SaMSDE AR (3/1) AR (3/2) 43600 26380 16360 62.477064 37.983 97630 74370 62890 15.097818 15.436 468200 330840 160600 65.698419 51.456 61880 76680 54362.5 12.148513 29.104 29110 19500 17880 38.577808 8.3076 53220 52590 37190 30.120256 29.283 50040 33540 22200 55.59524 33.750 PSO DE 29.33 Table 2. Best and (Worst) Functor values in 30 runs F PSO DE SaMSDE F_1 6.04453 e-005 8.69549 e-005 8.33852 e-005 0.000100901 0.00010096 F_2 5.56861 e-006 6.06769 e-005 4.78849 e-006 9.93975 e-006 F_3 0.00093023 0.00085359 0.086481 0.00993023 0.00089867	



(a)



Figure 2. NFEs taken to estimate the average of minimum fitness function value in 30 runs

6. Conclusions

In the present study we propose a scheme that dynamically adapts the mutation step size for better exploration and exploitation of the search space. The self adaptive mutation step size helps in increasing the diversity which in turn helps in balancing exploration and exploitation of the search space which finally helps in improving the solution quality and the convergence rate of an algorithm. This is evident from the empirical studies done in the present study. We are continuing our work towards the theoretical development of the proposed algorithms and extending them for solving constrained and real optimization problems..

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Function	Function Definition	D	Range	Optimum
Sphere	$f_1(x) = 10n + \sum_{i=1}^n (x_i^2 - 10\cos(2\pi x_i))$	30	[-5.12, 5.12]	0
Rastringin	$f_2(x) = \sum_{i=1}^n x_i^2$	30	[-5.12, 5.12]	0
Rosenbrock's	$f_{3}(x) = \sum_{i=1}^{n-1} \left[100 \left(x_{i+1}^{2} - x_{i}^{2} \right) + \left(1 - x_{i}^{2} \right) \right]$	10	[-30, 30]	0
Griekwank	$f_4(x) = \frac{1}{4000} \sum_{i=1}^n x_i^2 - \prod_{i=1}^n \cos(\frac{x_i}{\sqrt{i}}) + 1$	30	[-600, 600]	0
Step	$f_5(x) = \sum_{i=1}^{n} (x_i + 0.5)^2$	30	[-100, 100]	0
Ackly	$f_6 = -20 * \exp\left(2\sqrt{\frac{1}{n}\sum_{i=1}^n x_i^2}\right) - \exp\left(\frac{1}{n}\sum_{i=1}^n \cos(2\pi x_i)\right) + 20 + e$	30	[-32, 32]	0
Colliville	$f_7(x) = 100(x_2 - x_1^2)^2 + (1 - x_1)^2 + 90(x_4 - x_3^2)^2 + (1 - x_3)^2 + 10.1(x_2 - 1)^2 + (x_4 - 1)^2 + 19.8(x_2 - 1)(x_4 - 1)$	4	[-10, 10]	0

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Vitae



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